

# Coarse-grained, foldable, physical model of the polypeptide chain

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**Although nonflexible, scaled molecular models like Pauling–Corey’s and its descendants have made significant contributions in structural biology research and pedagogy, recent technical advances in 3D printing and electronics make it possible to go one step further in designing physical models of biomacromolecules: to make them conformationally dynamic. We report here the design, construction, and validation of a flexible, scaled, physical model of the polypeptide chain, which accurately reproduces the bond rotational degrees of freedom in the peptide backbone. The coarse-grained backbone model consists of repeating amide and  $\alpha$ -carbon units, connected by mechanical bonds (corresponding to  $\phi$  and  $\psi$ ) that include realistic barriers to rotation that closely approximate those found at the molecular scale. Longer-range hydrogen-bonding interactions are also incorporated, allowing the chain to readily fold into stable secondary structures. The model is easily constructed with readily obtainable parts and promises to be a tremendous educational aid to the intuitive understanding of chain folding as the basis for macromolecular structure. Furthermore, this physical model can serve as the basis for linking tangible biomacromolecular models directly to the vast array of existing computational tools to provide an enhanced and interactive human-computer interface.**

protein folding | self-assembly | biomimetic modular robotics | rotational energy barrier | conformational isomerism

**U**nderstanding protein folding pathways, predicting protein structure and the de novo designing of functional proteins have been a long-standing grand challenge in computational and structural biology. Although tremendous advances are being made (1), folded protein structures are very difficult to visualize in our mind due to their complexity and shear size. State-of-the-art computer visualization techniques are well developed and provide an array of powerful interactive tools for exploring the 3D structures of biomacromolecules (2–4). While increasingly complex molecules can be visualized with computers, the mode of user interaction has been mostly limited to the mouse and keyboard. Although the use of haptic devices is on the rise, there are only a few low-cost, specialized input devices particularly designed for interaction with biomacromolecules. Augmented-reality (AR) and immersive environments enhance user interaction experiences during the handling of existing visualization tools (2, 5, 6), but the physical models used in these environments are not flexible or precise enough to represent the conformational dynamism of polypeptides by themselves. There is a strong need for scaled, realistically foldable, but inexpensive, physical models to go hand-in-hand with the AR and other computer interfaces, while concomitantly taking better advantage of current computational capabilities.

Physical molecular models of organic small molecules and biomacromolecules with atomic representations have been around for many decades (7–17). Although early pioneers like Pauling and Corey’s scaled physical model of the polypeptide chain (11) helped to elucidate the molecular packing details of protein secondary structures (15, 17), these were nonflexible models and did not capture the inherent dynamism now known to exist in protein structures. Although there are a variety of physical molecular models commercially available (9, 10, 13, 14,

16), none have captured the true conformational degrees of freedom of the polymer chain, as the macromolecules have too many atoms, complex short-range and long-range conformational constraints, and specific folding behaviors. There are construction kits for  $\alpha$ -helices,  $\beta$ -sheets, and nucleic acids (14) that capture the scale and complexity of these molecules, but they are not flexible. Some models focus on chemical structures with multiple types of bonding (9) but are not made to scale. Other models spontaneously self-assemble into 3D molecules aided by internal magnetic fasteners (16) but are too simplistic to represent the folding of the polypeptide chain. Entire molecules of folded protein structures have also been generated with 3D printing, but these models do not explicitly represent the backbone and thus cannot be folded or unfolded.

Although many of the existing models are accurate with respect to physical dimensions (atomic radii, bond lengths, and bond angles), none is able to freely sample the bond rotational degrees of freedom that are needed to represent the motion of the polypeptide chain. The most dynamic representation reported is Olson’s articulated model that has been used to make flexible polypeptides by chaining the constituents through an elastic string, with the elasticity representing the pull between atoms (18). These models are flexible and can be folded into protein secondary and tertiary structures, but do not have the space-filling impact or a realistic representation of the dihedral angle rotational barrier that are so central to protein backbone behavior.

Despite these limitations, physical models have been rising in popularity (7, 8), as they play a critical role, both as educational tools and as aids to chemistry and biochemistry researchers to gain insight into protein-folding mechanisms. Physical models engage visuospatial thinking of biomolecules much more effectively than textbook images and computer screens can, via a process termed “tactile visualization” (19). Moreover, experiments with gaming interfaces like FoldIt have demonstrated that humans have superior 3D pattern matching skills than any existing software for solving challenging scientific problems (20, 21). We believe that this intuition and skill can be even more channelized while playing with physical, foldable models and may result in unexpected and surprising discoveries, as in the case of FoldIt.

With this vision in mind, we report here the design and fabrication of a tangible, coarse-grained, dimensionally accurate, physical molecular model of the polypeptide chain, which has the necessary degrees of freedom and bond rotational barriers to accurately emulate the backbone folding dynamics of the polypeptide chain. Our approach was to break down the component amino acids into constituent coarse-grained components linked

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by rotatable bonds. The flexibility of the backbone chain in our model has made it possible to readily build all of the common protein secondary structure elements. This model is a necessary first step toward a sophisticated computer input device that can manipulate and intuitively interact with computer visualization tools. It should ultimately be possible for these models to provide interactive dihedral angle information to computers while transitioning between various conformations. This would enable real-time feedback about the chain's conformational energy and direct comparison with known protein structures (structural homology searching). The model will serve as a first step in implementing an intuitive, computationally augmented physical model that can help people instinctively understand and hypothesize new details about the science of protein-folding pathways.

## Methods: Design and Testing of the Model

In real polypeptide chains, the bond rotations along the backbone are restricted, such that only certain bonds can rotate while others remain relatively rigid. Each amino acid monomer contains two backbone rotational degrees of freedom, the  $\phi$  and  $\psi$  dihedral angles (Fig. 1). When we consider the rigid and flexible backbone elements, the chain can be dissected into two repeating units: a set of four atoms confined to a rigid plane (forming the amide), and the  $\alpha$ -carbon atom, where two amides are connected via  $\phi$  and  $\psi$  bonds. Thus, the polypeptide backbone can be represented as an alternating copolymer of the amide unit and the  $\alpha$ -carbon unit. In our model, referred to as a Peppyptide, we emulate this basic structure of the polypeptide chain backbone by linking two types of units together: the amide units and the  $\alpha$ -carbon units ( $C_\alpha$ ), connected alternately at  $\phi$  and  $\psi$  bonds (Fig. 2 C and D). Thus, the simplest assembly that contains both  $\phi$  and  $\psi$  bonds is an  $\alpha$ -carbon linked to two amides. This forms an amide- $C_\alpha$ -amide arrangement in the model that we refer to as an amino acid diamide (Fig. 2A). We have also developed a third unit, a methyl-group unit (Fig. 2E) representing alanine, as a generic side-chain residue. Alanine is the smallest amino acid side chain, where the methyl group can approximate the impact of side-chain substitution and chirality on the general dynamics of a small peptide chain. Polyalanine has also been known to form  $\alpha$ -helices and  $\beta$ -sheets (22, 23).

Polypeptide backbone conformations are dominated by both short-range interactions about  $\phi$  and  $\psi$ , and longer-range intrachain hydrogen bonding interactions, as well as the interactions of the side chains. The Peppyptide model embodies both the short-range and long-range interactions of the backbone in addition to the steric hindrances of atoms that are within spatial proximity.

The factors most important for steric hindrances are the shapes and sizes of the constituent parts. By close analysis of protein crystal structures, the shapes of amide units (*trans*) and  $\alpha$ -carbon units (corresponding to L-amino acids) were designed (Fig. 2A). The most widely accepted values of interatomic distances have been used for the atomic-scale dimensions of the units (Fig. 2B) (24). All parts were drawn to scale with a scale factor of  $1 \text{ \AA} = 0.368^\circ$  in a computer-aided design (CAD) software (Fig. 2 C–E). The  $\phi$  and  $\psi$  bonds, which are the linkages between the amide and  $\alpha$ -carbon units, were implemented with freely ( $360^\circ$ ) rotating nut-and-screw arrangements. Rotational barriers were also included to reproduce the dihedral angle preferences observed in protein structures (see below). As the constituent atoms of each of the units need to be within their covalent bonding distances, the bonding atoms were cut along specific planes, as had been previously done with the Corey-Pauling-Koltun (CPK) and other models (11).

Theoretically, the atom size for the elements in the backbone chain, namely the model radii ( $R_M$ ), in any model should be equal to their Van der Waals radius ( $R_{VDW}$ ). However, in a dynamic physical model, the  $R_M$  needs to be a fraction of  $R_{VDW}$  for the chain to move freely and avoid getting

interlocked with itself. This was examined by checking for steric clashes in a CAD software using a 3D drawing of the alanine diamide molecule assembled using Peppyptide model units.  $R_M$  was varied from  $0.6 R_{VDW}$  to  $0.8 R_{VDW}$  (Fig. 3C and SI Appendix, Fig. S1), and it was found that  $R_M = 0.7 R_{VDW}$  is the largest size possible for representing hard spheres while maintaining access to the entire conformational landscape accessible by polypeptides.

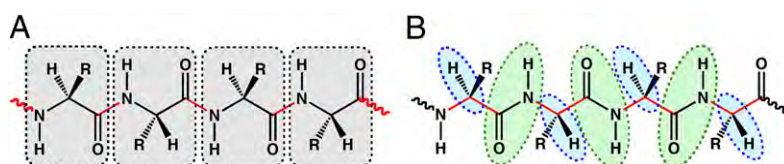
The backbone dihedral angles in polypeptide chains do not rotate freely. There are barriers to rotation about both  $\phi$  and  $\psi$  that limit the conformational flexibility of the chain, which is a result of the local bonding geometry, steric and electronic effects (25). We therefore introduced a conformational bias into each rotatable bond in the backbone of the model. The favored dihedral angles ( $\phi$ ,  $\psi$ ) in polypeptides are well known from experimental data and are typically illustrated in a Ramachandran plot (25). The densest regions of the plot, that is, the most favorable regions, are low-energy positions of dihedrals of the polypeptide backbone (Fig. 3D). These preferred regions mostly correspond to the  $\alpha$ -helix (left- and right-handed) and the  $\beta$ -sheet conformations—the secondary structures universally found in proteins.

To represent these barriers within the physical model, it was necessary to decouple  $\phi$  and  $\psi$  from each other and to study their behavior separately. The information from the Ramachandran plot was decoupled to get independent values of  $\phi$  and  $\psi$  over the full range of rotation ( $-180^\circ$ ,  $180^\circ$ ) (Fig. 3 A and B). We used data from  $\sim 78,000$  known protein structures in the Protein Data Bank (PDB) because these data are a direct manifestation of the favored angles adopted in proteins. For comparison, we also generated a Ramachandran energy map with OPLS 95 (optimized potentials for liquid simulations) force fields in the Maestro framework for alanine dipeptide, where the energy minima mostly clusters around  $\phi = -70^\circ$  and  $-140^\circ$  (Fig. 3E). However, these calculated energies are an indirect measurement of the same effect as they reflect only very local interactions. As we wanted to incorporate the effects of both short-range and long-range interactions in the physical model, we used the data from the PDB histogram instead of the minima in the energy maps to design the rotational barriers.

The decoupled  $\phi$  and  $\psi$  distributions giving preferred angles for  $\phi$  and  $\psi$  (Fig. 3 A and B) were calculated from  $\sim 59$  million ( $\phi$ ,  $\psi$ ) values obtained from 77,873 protein structure files from the PDB (crystallography and NMR structures only). The four peaks obtained (two for  $\phi$ ; two for  $\psi$ ) correspond to the darkest regions of the Ramachandran plot for  $\alpha$ -helix and  $\beta$ -sheet conformations, and denote the corresponding minimum energy configurations. This analysis shows that the  $\phi$ -peaks are  $56^\circ$  apart (at  $-62^\circ$  and  $-118^\circ$ ) and  $\psi$ -peaks are  $180^\circ$  apart (at  $-42^\circ$ ,  $138^\circ$ ). There is a third  $\phi$ -peak at  $\sim 61^\circ$  that corresponds to left-handed helices, which is not represented in this version of the model. The peaks in the  $\phi$  and  $\psi$  distributions were each fit to Gaussian distribution (Fig. 3A) to facilitate their approximation in the physical model.

To introduce these dihedral angle preferences, or rotational barriers into the physical model, we used a customized circular magnet array for each  $\phi$  and  $\psi$  bond. Magnet arrays can be quite intricate and can produce a wide variety of mechanical interactions (26, 27). Magnets are attractive choice in this application because they are noncontact, frictionless, cheap, passive (need no power to operate), exhibit strong coupling behavior, and can generate Gaussian barriers.

In Peppyptides, we reproduced the conformational biasing due to rotational barriers by two separate arrangements of magnets for  $\phi$  and  $\psi$ , respectively, that work in unison to form a physical rotation barrier (Fig. 4). By arranging small, powerful neodymium magnets across the rotational interfaces (Fig. 4, Left), certain bond rotation angles (or angle ranges) are preferred by the model during the  $360^\circ$  rotation of the  $\phi$  or  $\psi$  bonds. Thus, we are able to embody, with reasonable precision, the natural torsional angle biases for the entire landscape of the Ramachandran plot in the model. Based on the distribution functions of  $\phi$  and  $\psi$ , the magnets are positioned  $56^\circ$  and  $180^\circ$  apart, respectively (Fig. 4A for  $\phi$  coupled faces, and Fig. 4B for  $\psi$  coupled faces). In our design, the most stable conformations of both  $\phi$  and  $\psi$



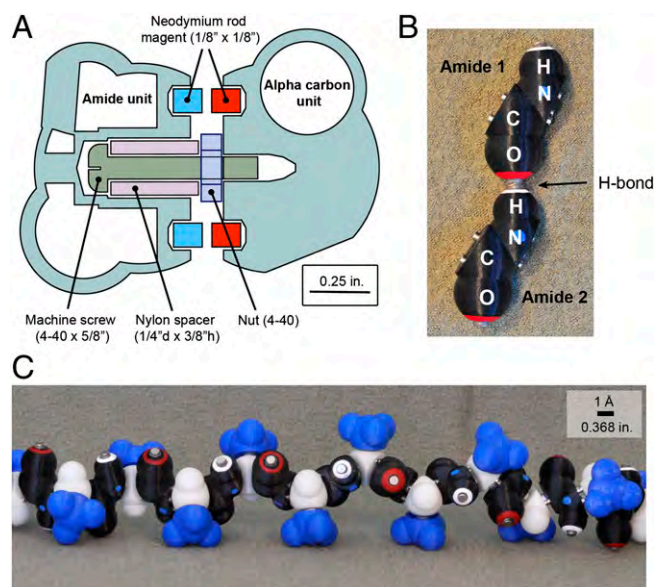
**Fig. 1.** Representations of the repeating units of the polypeptide chain. (A) A repeating homopolymer of amino acid units connected by amide bonds (red), (B) an alternating copolymer of rigid amide (green) and  $\alpha$ -carbon (blue) units connected by the rotatable bonds  $\phi$  and  $\psi$  (red).





**Fig. 4.** Enforcing rotational barriers on the  $\varphi$  and  $\psi$  bonds using circular magnet arrays; N, north pole; S, south pole. (A) (Left) The coupled faces for  $\varphi$ , simulating the rotational constraints on  $\varphi$ ; peaks are  $56^\circ$  apart. (Center)  $\varphi$ -faces of the amide and  $\alpha$ -carbon units. (B) (Left) The coupled faces for  $\psi$ , simulating the rotational constraints on  $\psi$ ; peaks are  $180^\circ$  apart. (Center)  $\psi$ -faces of the amide and  $\alpha$ -carbon units. (A and B) (Right) The measured energy landscape for  $\varphi$  (Upper) and  $\psi$  (Lower) in the model corresponding to magnet arrangements (red), overlaid with the distribution of  $\varphi$  and  $\psi$  from protein structures (blue) for performance comparison; (Insets) the coupling of interface magnets that lead to the respective peaks in the model. blue ( $\omega$ -face). red ( $\psi$ -face).





**Fig. 5.** Peppytide model assembly. (A) Bore dimensions and assembly plan for the amide unit and  $\alpha$ -carbon unit joint (cross-section view drawn to scale); the same scheme was used for the  $C_{\alpha}$ -CH<sub>3</sub> joint. (B) Representation of a hydrogen bond between distal amides. (C) A Peppytide homopolymer (polyalanine); black part, amide unit; white part,  $C_{\alpha}$  unit; blue part, methyl group unit; red ring, oxygen; white ring, hydrogen; blue dot, nitrogen.

have also successfully folded longer Peppytide chains into several known protein conformations, including a minimal  $\beta\alpha$  motif (28-mer, pid:1FSD) (40), and fish osteocalcin (chain A; 45-mer pid:1VZM) (Fig. 6D and *SI Appendix, section S6 and Fig. S14*). It demonstrates that, as expected, a generic Peppytide chain can readily adopt a variety of specific folds. They can be used to make extremely complex structures, the folding of which is highly instructive.

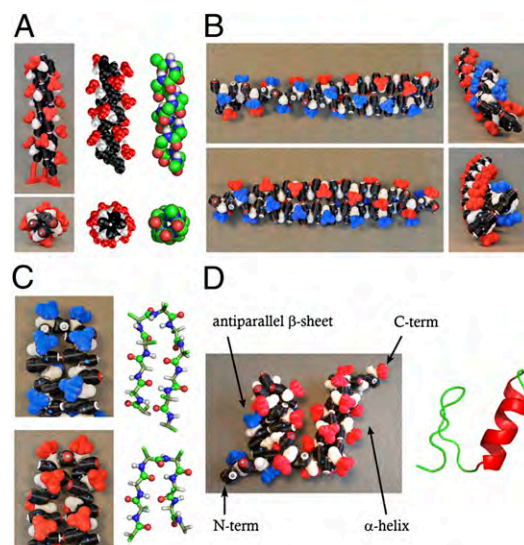
### Self-Folding and Biomimetic Modular Robotics

Although the current Peppytide model is a good tool for studying and teaching polypeptide chain folding, it also illustrates a fundamental architectural principle ubiquitous in biology: that a linear chain of modular units can be configured into a fantastic variety of 3D shapes. There is growing interest in translating this concept to the macroscopic scale to create reconfigurable objects from a universal set of modular units. The intersection of microelectronics, pervasive computing, and growing interests in biolocomotion have paved a path for the emerging field of biomimetic robotics with multimodular units working distributively to accomplish a single task. Advances are being made to fold a generic linear chain or a flat sheet into almost any 3D shape, to ultimately provide “programmable matter” (41–48). Engineers have created complex, dynamic multiunit systems that operate electronically and can interface with one another and/or a computer. These robots enable dynamic conformational information to be sent to a computer base station or to each other in real time. With the advent of miniaturized actuating technologies, this has broader impacts for future computational models for studying molecules, especially folding pathways and protein receptors, if one molecule could communicate with another wirelessly and convey its structure. Moteins, a 1D string of simple modular (polygonal or polyhedral) robots, have been shown to programmatically fold and self-assemble into 3D shapes (42). Posey is a physical construction kit that captures the shape of the assembled objects and virtually represents that in the host computer (45, 46). PolyBot, a modular robot, has been used to emulate a variety of gaits (e.g., snake-like horizontal sinusoidal

motion, caterpillar-like vertical climbing motion, etc.) by propagating a wave signal through the modules (47). Inspired by paper origami, programmable folding has been used to direct the folding of a 2D sheet into various 3D shapes (43). In close analogy to protein folding, these examples have a fundamentally flexible, almost universal ability to form any given arbitrary 3D structure from a standard set of building blocks. In this respect, the Peppytide model reported here represents an important step to bridge the gap between structural biology and macroscopic design—an architectural bridge across great length scales to directly adopt nanoscale, macromolecular structural design principles to human-scale objects.

### Conclusions

Despite previous efforts to build interactive physical models of biomacromolecules, there still lacks a mechanically faithful reproduction of the polypeptide chain that captures the mechanical flexibility, degrees of freedom, short- and long-range (nonbonding) interactions, all of which are essential features of the molecular system. The Peppytide model developed here reproduces several critical aspects of the natural system that impact chain dynamics including the following: (i) dimensional accuracy of bond lengths and bond angles, (ii) a faithful representation of the short-range rotational barrier imposed on all of the backbone dihedral angles, and (iii) long-range stabilization resulting from intrabackbone hydrogen bonding. The model is foldable into stable secondary structures of proteins with considerable accuracy, and is an excellent tool with which to intuitively understand the process of biopolymer chain folding and unfolding of tertiary structures. Because folding of linear polymer chains is a fundamental architectural concept ubiquitous in biology, tools like the Peppytide



**Fig. 6.** Secondary and tertiary structures formed from the Peppytide model. (A) Comparison of a 13-mer polyalanine  $\alpha$ -helix ( $R_M = 0.7 R_{VDW}$ ): (Left) Peppytide physical model (alanine side chains in red); (Center) Peppytide in CAD representation with theoretically ideal values of  $\phi = -62^\circ$ ,  $\psi = -42^\circ$ ; (Right)  $\alpha$ -helix from crystal structure (leu-zipper pid:2ZTA, residues 16–28) (Upper: front view; Lower: top view). (B) Two strands of polyalanine Peppytide model folded into  $\beta$ -sheet conformations (with blue alanine side chains in one strand, and red in the other): (Upper) antiparallel, (Lower) parallel; the views to the Right show the natural curvature of the sheets. (C)  $\beta$ -turns: (Upper) type I in Peppytide compared with a turn in pid:1AAR, residues 4–14. (Lower) Type II in Peppytide compared with a turn in pid:3KVD, residues 221–228. (D) De novo  $\beta\beta\alpha$  motif (pid:1FSD), a 28-mer; blue side chains indicate N-term; (Right) protein ribbon structure, green indicates loop and  $\beta$ -sheet, and red indicates  $\alpha$ -helix.

model promise to play an important role to teach and conceive the concepts of protein folding.

The simple design of the model makes it ideal for further elaboration. An obvious next step is to expand to the full set of amino acid side chains, so that a complete protein tertiary structure can be folded. Potential further improvements to this model would be the use of softer materials, which would allow the model to sample more of conformational space while using  $R_{VDW}$  closer to 1, and to perhaps elaborate on them to include representations of electrostatic or hydrophobic forces. Sensor, actuator, or microprocessor control could also be incorporated to create a more realistic, user-friendly input/interaction device for computational tools. One application might be to make Peppytide “display” the folding pathway as a function of time, given the ability to self-fold through actuators. It should also be possible to create a model with assignable and distinct bond angles for each backbone dihedral angle, which would bias them to fold into a predetermined structure. Getting multimaterial 3D printed models to generate flexible structures or to self-fold is also an exciting possibility (49, 50).

Although polypeptides are a compelling first target for this type of model, the work is not limited to this class of compounds. Similar models of other macromolecular systems, including polynucleotides, peptidomimetics (e.g., polypeptoids and  $\beta$ -peptides), as well as synthetic polymers (e.g., Kevlar, conducting polymers, polystyrene, polyethyleneoxide, etc.), could be made to inform the emerging field of protein-mimetic nanostructures.

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# **A coarse-grained, foldable, physical model of the polypeptide chain**

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## **Supporting Information**

### **Table of Contents**

<b>S1.</b>	<b>Comparison of fractional Van der Waals radii.....</b>	<b>2</b>
<b>S2.</b>	<b>Model specifications .....</b>	<b>4</b>
<b>S3.</b>	<b>STL files for 3D printing .....</b>	<b>6</b>
<b>S4.</b>	<b>Methodology for model printing and assembly .....</b>	<b>7</b>
<b>S4.1.</b>	<b>3D printing.....</b>	<b>7</b>
<b>S4.2.</b>	<b>Peppytide model assembly.....</b>	<b>8</b>
<b>S5.</b>	<b>Determination of the rotational energy barrier profile for the circular magnet array .....</b>	<b>12</b>
<b>S6.</b>	<b>Secondary and tertiary structures in Peppyptides.....</b>	<b>14</b>
<b>S7.</b>	<b>Supplementary movie .....</b>	<b>18</b>

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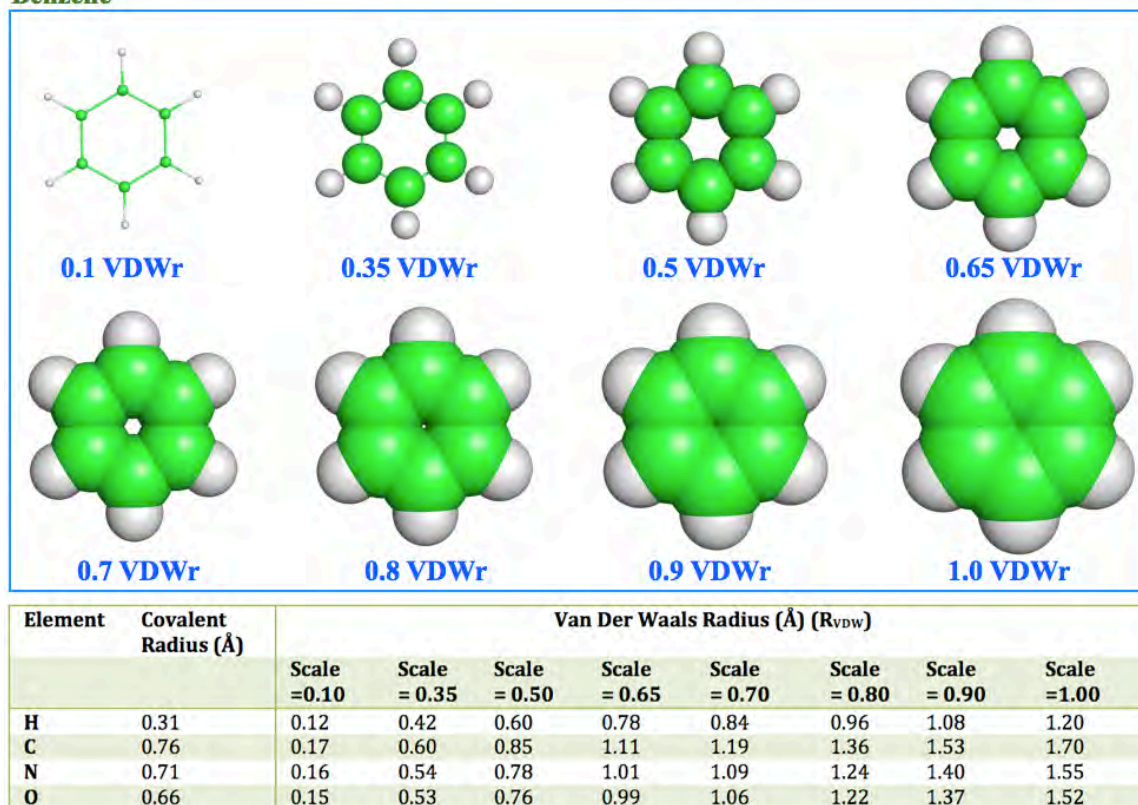
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## S1. Comparison of fractional Van der Waals radii

We implemented Peppyptides with atom sizes equal to 0.7 of the Van der Waals radius ( $R_{VDW}$ ). This particular size avoids the unrealistic hard sphere overlap of the atoms, while maintaining access to the entire conformational landscape accessible by polypeptides. This allows the entire feasible region of the Ramachandran plot to be spanned by the Peppyptide model while being big enough to experience realistic steric hindrances as the atoms move. We observed that with atomic radii smaller than 0.5  $R_{VDW}$  the steric impact of the atom sizes is lost (**Fig. S1**), while atoms close to 0.8  $R_{VDW}$  are too big because of unrealistic overlaps, resulting in unrealistic locking of the structure. Hence we focused on a window of 0.6–0.8  $R_{VDW}$ , and analyzed the steric hindrance landscape for 0.6, 0.7 and 0.8  $R_{VDW}$  (**Fig. 3C**), where 0.7  $R_{VDW}$  proved to be the optimal size. **Fig. S1** gives an idea of the relative sizes of the various fractional radii values.



## Benzene



**Fig. S1:** (Lower) A comparison of the covalent bond radii and the various fractional Van der Waals radii of the atoms found in the polypeptide chain. (Upper) Benzene at different fractional Van der Waals radius values.

## S2. Model specifications

We have taken special care to keep the physical model as light as possible, so that the gravitational force on the overall chain is minimized. The weight of each part was determined (Table S1). Before weighing, the 3D-printed parts were dried overnight in the desiccator to ensure that they were completely dry.

**Table S1: Details of the parts used in the Peppytide model**

Part-name	Subparts	Description	Weight (g)	Total (g)
Amide unit	3D printed amide group	ABS plastic	4.53	
	2 H-bond Neodymium rod magnets	For O and H; 3/16"D x 1/8"H; pull force = 2.49 lbs.		
	5 Neodymium rod magnets	Neodymium rod magnets. For representing rotational barriers in dihedrals (3 for phi; 2 for psi); 1/8"D x 1/8"H; pull force = 1.43 lbs.	0.94 (0.19 each)	
	<b>Amide total =</b>			<b>5.47 g</b>
Alpha-carbon unit	3D printed alpha-carbon unit	ABS plastic	3.04	
	4 Neodymium rod magnets	Neodymium rod magnets. For representing rotational barriers in dihedrals (2 for phi; 2 for psi); 1/8"D x 1/8"H; pull force = 1.43 lbs.	0.74 (0.19 each)	
	<b>C<math>\alpha</math> total =</b>			<b>3.78 g</b>
Covalent Bonds (3 bonds to connect the alpha carbon to 2	3 Screws	Pan-head machine screw 5/8"H, 4-40 thread	1.22 (each bond)	
	3 Nuts	Machine screw nuts;		

Part-name	Subparts	Description	Weight (g)	Total (g)
amides, and one side chain residue)		3/32"H, 0.25"D, 4-40 thread		3.66 g
	3 Spacers	Nylon spacer; 0.25"D x 3/8"H		
	3 bonds total =			
Methyl group Unit	3D printed part	ABS plastic	2.68	2.68 g
	Methyl group total =			
1 complete monomeric subunit (1 amide, 1 C $\alpha$ , 1 methyl group, 3 bonds)			15.59	15.59 g
Monomer subtotal =				
An alanine 9-mer Peppytide model			140.31	140.31 g
Model total =				

**Table S2: Parts and suppliers**

Part	Supplier	Part Number
uPrint Plus Model Material, P430 Color Model Material Spools (each 30 cu. in) – Package of 5 (red, blue, black, ivory)	Dimension (Paton Group)	340-21200
uPrint P400-SR Soluble Support Material (each 30 cu. in) – Package of 5	Dimension (Paton Group)	345-20005
Screw	McMaster-Carr (mcmaster.com)	91735A109
Nut		91841A005
Spacer		94639A202
Magnet (rotational barrier)	Magcraft	NSN0658
Magnet (H-bond)	K&J Magnetics, Inc. (kjmagnetics.com)	D32-N52



### S3. STL files for 3D printing

The 3D printable stereolithography (STL) files of the parts in the model are provided here (as .txt files), along with detailed instructions for assembly in the next section to enable anyone to build these models themselves. The STL files can be used for 3D-printing with any color of choice using any 3D printer. The following STL files are provided as supplementary materials:

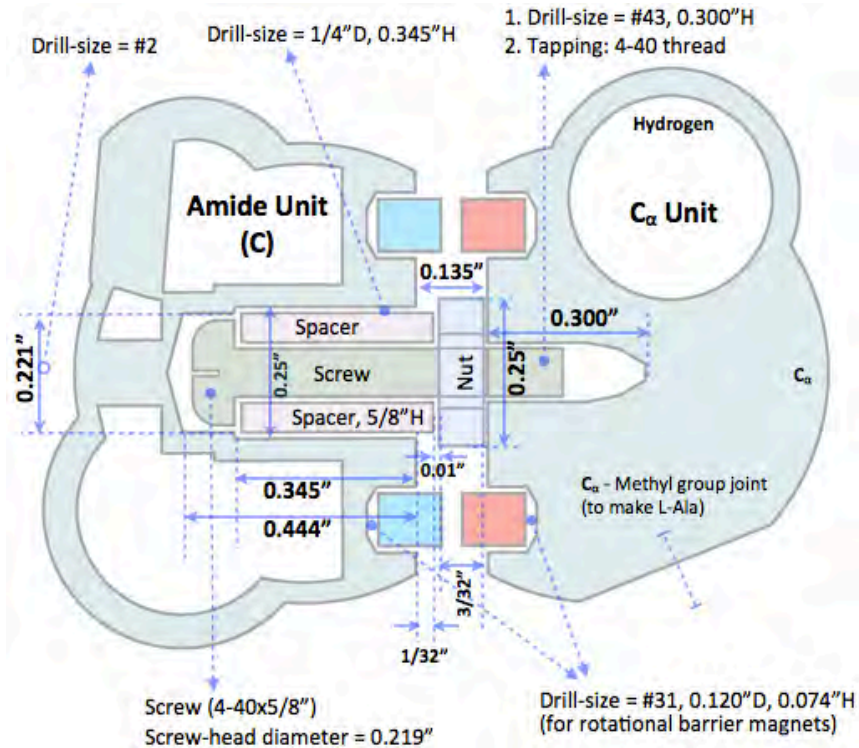
1. Amide STL file (Dataset S1: filename PNAS\_201305741\_s5.txt) – amide unit consisting of the hydrogen, nitrogen, carbon ( $C_O$ ) and oxygen atoms
2. cAlpha STL file (Dataset S2: filename PNAS\_201305741\_s6.txt) – alpha carbon unit consisting of the alpha-carbon ( $C_\alpha$ ) atom and the hydrogen atom
3. methylGroup STL file (Dataset S3: filename PNAS\_201305741\_s7.txt) – the residue (– $CH_3$  group) corresponding to the amino acid Alanine.

To 3D-print, replace .txt in the filenames with .stl before sending it to the printer. These STL files are of acceptable resolution and should provide a smooth surface when printed at the same scale (1x). However, files of higher resolution may be provided upon request.

## S4. Methodology for model printing and assembly

### S4.1. 3D printing

The 3 plastic coarse-grained atom parts (amide unit, alpha carbon unit, methyl group unit) were drawn to scale using the CoCreate Modeling 2008, a CAD modeling software (version 16.0, PTC) (**Fig. 2**). The drawing files were then converted to stereo lithography (STL) files that were used for 3D-printing of the parts. A Dimension uPrint Plus 3D printer was used to print the parts using ABS plastic. It uses Fused Deposition Modeling (FDM) technology to build a 3D structure on a layer-by-layer basis using ABS plastic material for the model, and a soluble plastic as a scaffold to support the model structure while it is being printed. Following this, the printed parts were soaked in a sodium hydroxide based solution for 4-6 hours, to dissolve the supporting plastic materials. The parts were then rinsed well with water, and desiccated overnight to make them completely clean and dry. At this point, the dried parts are ready for drilling and assembly (**Fig. S2**). The overall process, from printing to drying, takes about 3-4 days for making a 9-mer model. Printing time varies proportionately depending on quantity.



**Fig. S2:** Detailed drilling and assembly plan of Peppytide

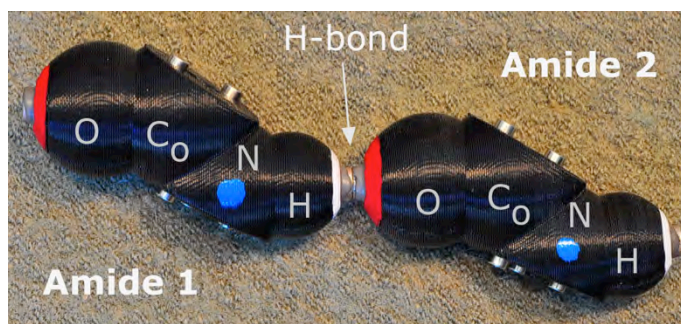
## S4.2. Peppytide model assembly

The Peppytide model can be assembled using the following steps:

**Step 1: Part printing.** 3D-printing of 3 types of units as described above: amide, alpha-carbon, methyl-group (printing, soaking, drying). (see supplementary Datasets S1-S3 for the parts, Section S3). See **Table S1** for details on magnets, screws, spacers and nuts needed for assembly.

### Step 2: Amide unit preparation.

- a. Installation of the H-bond magnets.** Sand the bottom face of the H-bond magnets (3/16" x 1/8") with 220 grit sandpaper to roughen the surfaces for effective adhesion. Next, glue the magnets onto the amides using Epoxy (JB-weld); O with North pole up; H with South pole up (**Fig. S3**). Leave for 24 hours for setting and drying.



**Fig. S3:** The 4 atoms of the amide units; the hydrogen-bond.

- b. Labeling.** Color-code the amide units with red-ring for oxygen, white-ring for hydrogen, and with blue-dot for nitrogen atoms in the amide units (**Fig. S3**).
- c. Drilling dihedral rotational barrier magnet holes.** Enlarge the magnet holes by drilling to a depth of 0.074" (drill size #31, 0.120") in the amide units (**Fig. S2**). This hole-depth will allow each magnet to protrude by ~0.051". Slightly undersized guide holes are provided to minimize the amount of material removed by the drill.
- d. Drilling the bond holes.** Enlarge the central bond holes (C and N atoms) by drilling to a depth of 0.345" (drill size 0.250") in the amide units (**Fig. S2**). This hole-depth will allow the nylon bond spacer to protrude by 1/32". Slightly undersized guide holes are provided to minimize the amount of material removed by the drill.



### Step 3: Alpha carbon unit preparation.

- a. **Drilling the rotational barrier magnet holes.** As with the amides, enlarge the magnet holes by drilling to a depth of 0.074" (drill size #31, 0.120") in the alpha carbon units (**Fig. S2**). This hole-depth will allow each magnet to protrude by 0.051". The final bore diameter of 0.120" is intentionally undersized to allow a press-fit of the 1/8" diameter magnets (see step 4 below).
- b. **Drilling the bond holes.** Drill to a depth of 0.300" (drill size #43, 0.089") on the 3 faces (N-face, C-face and the side-chain-face) of the alpha-carbon units. Guide holes are provided, by design (**Fig. S4**).
- c. **Tapping the bond holes.** After drilling the central bond holes, tap them with 4-40 threads to their full depth (**Fig. S4**).



**Fig. S4:** Alpha carbon bond guide holes

**Step 4: Addition of the rotational barrier magnets.** Press fit the dihedral magnets (1/8" x 1/8") into alpha carbon units (with North pole up) and in amide units (with South pole up) ( **Fig. S5**).



**Fig. S5:** Steps of assembly. (Upper) amide unit; (Lower) alpha carbon unit.

**Step 5: Bond linkage assembly.** Assemble screws, nuts, and spacers for bond linkages (**Fig. S6A**). There are 3 such bonds per monomer unit:  $C_\alpha$ -Amide(N),  $C_\alpha$ -Amide(C), and  $C_\alpha$ -Side-chain.



(A) assembled bond

(B) parts and bonds

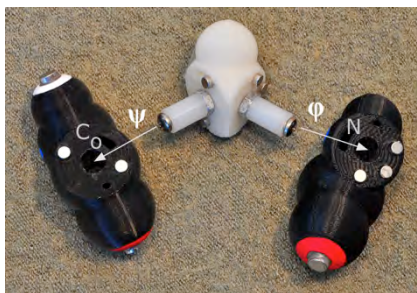
**Fig. S6:** Assembled bonds and related parts that need to be linked per repeating monomer unit.

**Step 6: Alpha-carbon bond assembly.** Assemble bonds into the  $C_\alpha$  units by screwing the bonds into the alpha carbon and securely tightening the nut, while leaving a slight gap to allow free rotation of the spacer (**Fig. S7**).



**Fig. S7:** Alpha carbon unit with bond linkages

**Step 7: Backbone assembly.** Push-fit bond linkages from  $C_\alpha$  units into amides (**Fig. S8**). The bonds will bottom out into the amide bores.



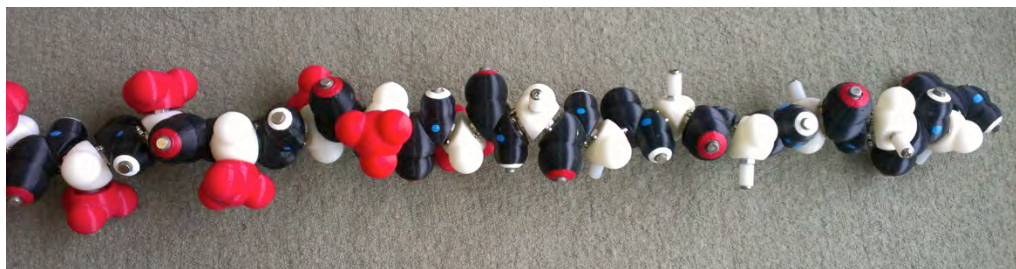
**Fig. S8:** Connecting the alpha carbon unit with the two faces of amide units.

**Step 8:** Repeat steps 6 and 7 to make the entire backbone chain of alternating amide unit and alpha-carbon unit (**Fig. S9**).



**Fig. S9:** Completed backbone assembly of the Peppyptide model.

**Step 9: Adding side chain residues.** Lastly, press-fit the methyl groups onto the 3<sup>rd</sup> bond linkages of the C <sub>$\alpha$</sub>  units in the backbone chain (**Fig. S10**).



**Fig. S10:** Addition of the side chain methyl units (red).

Step 9 gives the final assembled Peppyptides chain.

We took care to make the holes and the drilling depths accurate up to 3 decimal places, while correcting for the errors due to the tolerances of the 3D printer and the press-fitting technique. The goal was to have 1/32" of the spacer protruded from the amide N/C faces to get the correct effective bond lengths, and to have the dihedral magnets protrude at most 0.051"-0.054" to avoid collision during rotation, while retaining enough proximity for effectual magnetic attractive forces. We experimented to get the desired drilling depths of holes by using drilling jigs with adjustable heights (**Fig. S11**). The drilling jig speeds up the time required for assembly by a factor of ~5.



(A) The drill at the top; with 1/4" compressed air line to rapidly clear away drilled materials for a smooth hole.



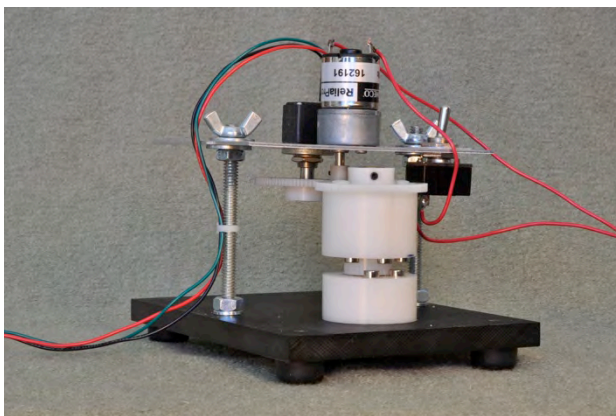
(B) Precision control of drill depth by adjustment of screw stops.

**Fig. S11:** Drilling jig with adjustable height enables precision depth control.



## S5. Determination of the rotational energy barrier profile for the circular magnet array

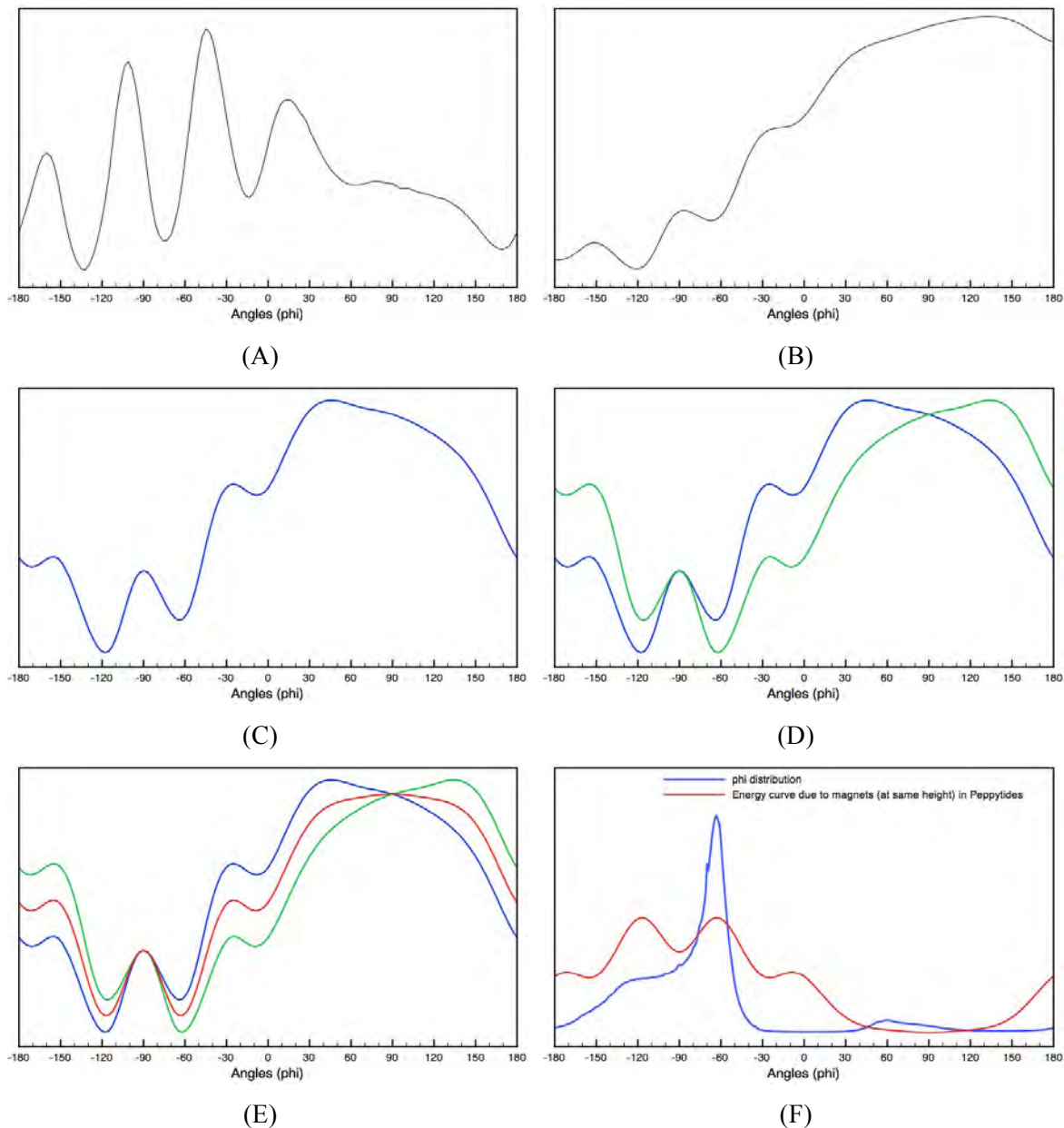
We quantified the rotational energy barrier profile as a function of bond angle due to the circular phi/psi bond magnet arrays, and compared the peaks with that from the real protein structures (**Fig. 4**). A sensitive torqometer was constructed from a DC motor and a rotary encoder. We measured the current (I) drawn at constant voltage (V) by each pair of the magnet arrangements over a 360° cycle, using a DC motor and microcontroller equipped with a low-side current sensor (1 ohm resistor) and an analog to digital converter (**Fig. S12**). Data for 10 rotation cycles were gathered for each of the phi and psi pairs. This data were then converted to the respective energy values. As work done,  $\Delta W = VIt$ , the current data were integrated as a function of rotation angle to get the relative energy wells, with subsequent inversion to get the energy-peak curve. We averaged the data over the forward and reverse directions (clockwise and anti-clockwise) to remove any directional bias in the system.



**Fig. S12:** A simple torqometer was used to monitor current drawn by the rotational barrier magnet arrays as a function of bond angle.

We used the following steps to process the raw data in order to plot the energy peaks:

- Imported the raw data and averaged over all cycles (**Fig. S13A**)
- Integrated the data to get energy-well curve for anticlockwise rotation (**Fig. S13B**) and normalized the data (**Fig. S13C**)
- Similarly, obtained the energy well curve for clockwise rotation (**Fig. S13D**), and averaged the two curves in two directions to correct for rotational bias (**Fig. S13E**)
- Inverted the curve to get the energy-peak curve (red) and compared it with the data from protein data bank (blue) (**Fig. S13F**, also see **Fig. 3**)



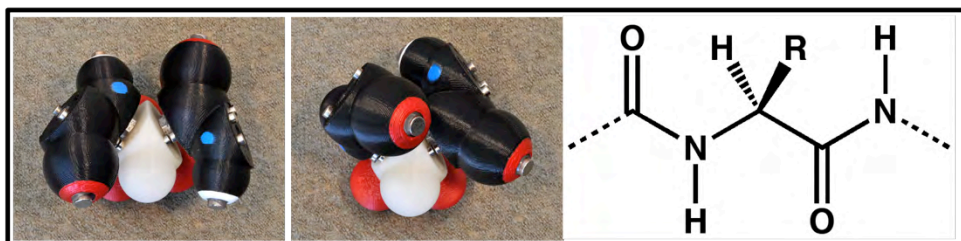
**Fig. S13:** Data processing steps in converting the torqometer current data into the rotational barrier data. (A) Raw data averaged over 10 cycles (clockwise); (B) integrated plot; (C) normalized, scaled (zoomed-in) integrated curve; (D) similarly, integrated plot for anticlockwise rotation (green); (E) averaging clockwise and anticlockwise data, to correct for directional bias (red) to get plot for energy wells; (F) Inverted curve from E to get the energy peak curve, superimposed with psi distribution curve from PDB data files for comparison (peaks at  $-62^\circ$  and  $-118^\circ$ ).

## S6. Secondary and tertiary structures in Peppytides

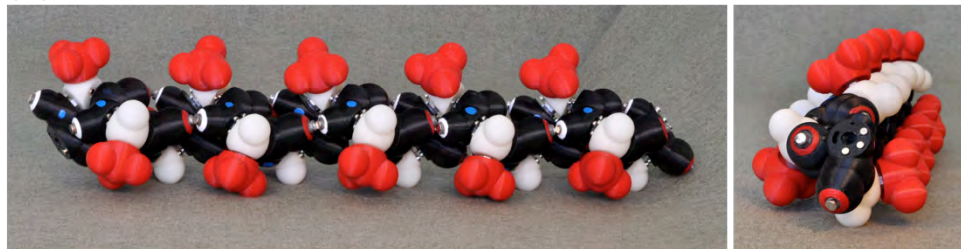
We tested the Peppytide model by folding it manually into various secondary and tertiary structures. In **Fig. 6**, we reproduced the most prevalent secondary structures found in nature: the right-handed  $\alpha$ -helix, the  $\beta$ -sheets and type I and type II  $\beta$ -turns. We also assembled an entire tertiary structure of  $\beta\beta\alpha$  motif.

A few additional structures made are provided here. The simplest and smallest possible unit with one phi and one psi bond is an “alanine diamide” unit. The unit is shown in the most favored orientations, for both the  $\alpha$ -helix and  $\beta$ -sheet (**Fig. S14a**) conformations. Besides the most common  $\alpha$ -helix, we have also made the tighter  $3_{10}$  helix, and the looser  $\pi$ -helix (**Fig. S14b** and **c** respectively). This demonstrates that the model is able to withstand the twisting and folding flexibility needed to exhibit the entire range of polypeptide backbone dynamics. Lastly we show the model folded into a much longer chain of 45 amino acids (fish bone Osteocalcin, chain A pid:1VZM) which illustrates that the model has the capability to make meaningful polypeptide tertiary structures of small but considerable length in which to explore various structures and their intermediates.

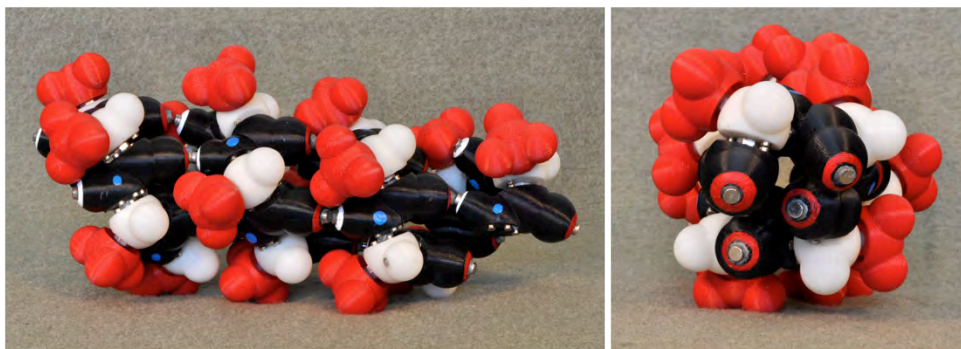
(a)



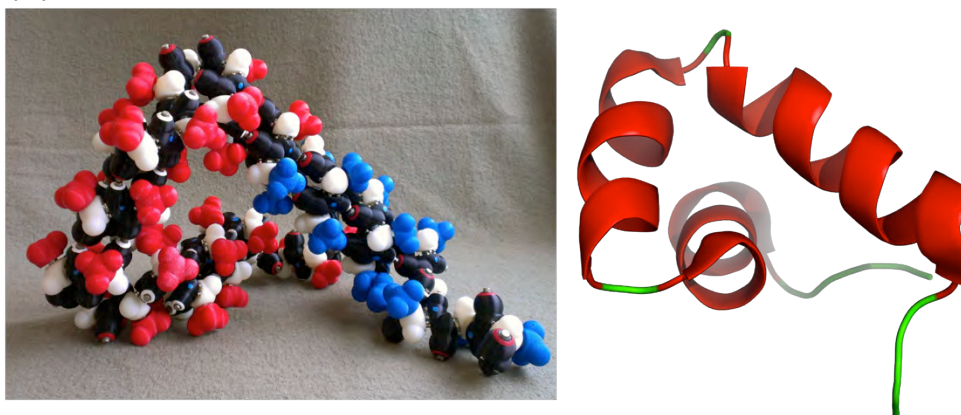
(b)



(c)



(d)

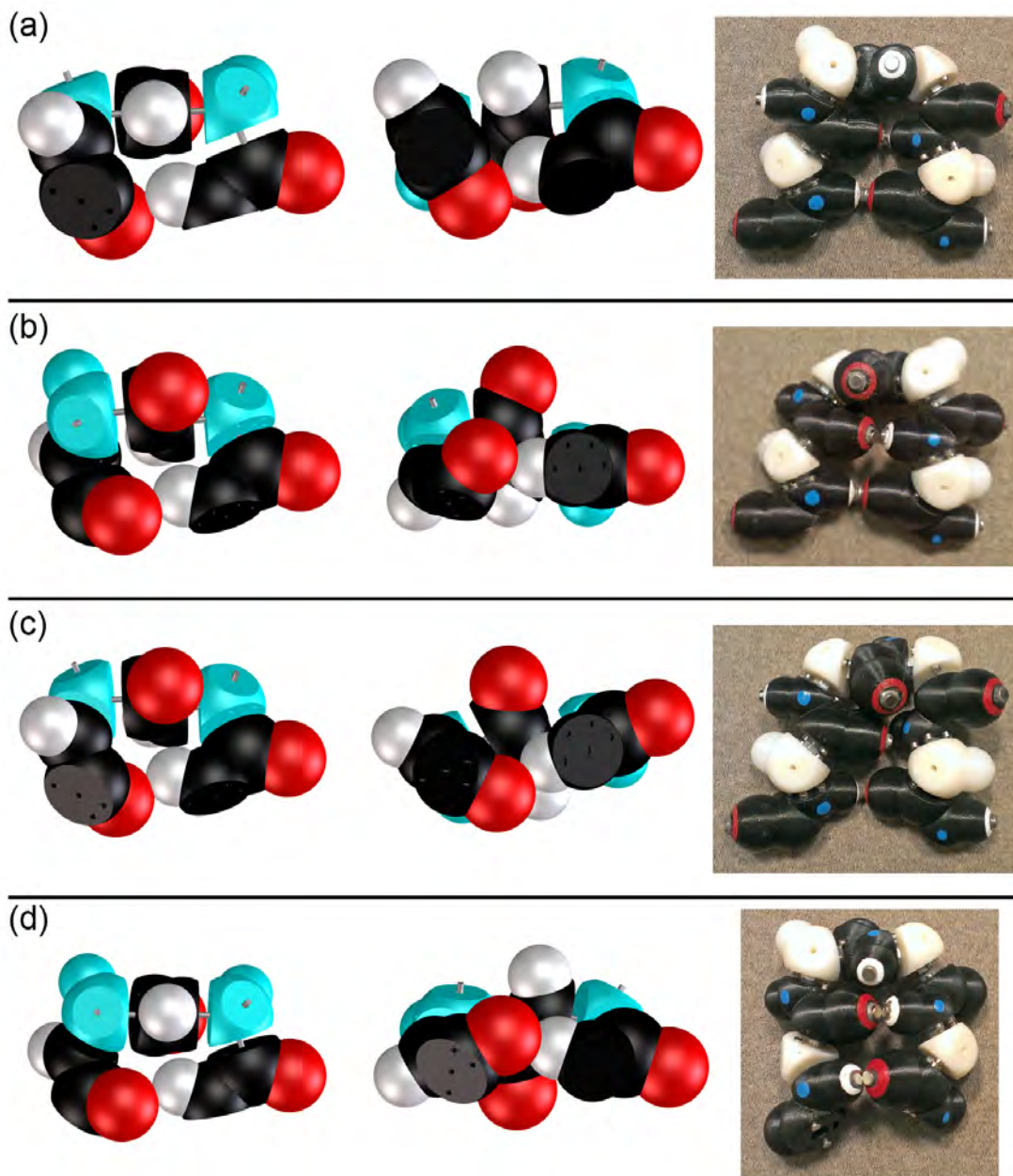


**Fig. S14:** Secondary and tertiary structures in Peppyptides. (a) Alanine diamide: (left)  $\beta$ -sheet orientation, (center)  $\alpha$ -helix orientation, (right) 3D structure. (b)  $3_{10}$  helix. (c)  $\pi$ -helix. (d) Fish osteocalcin (chain A), a bone protein with 45 amino acids (pid:1VZM); blue side chains indicate N-term; (right) protein structure cartoon, green indicates loop, and red indicates  $\alpha$ -helix.



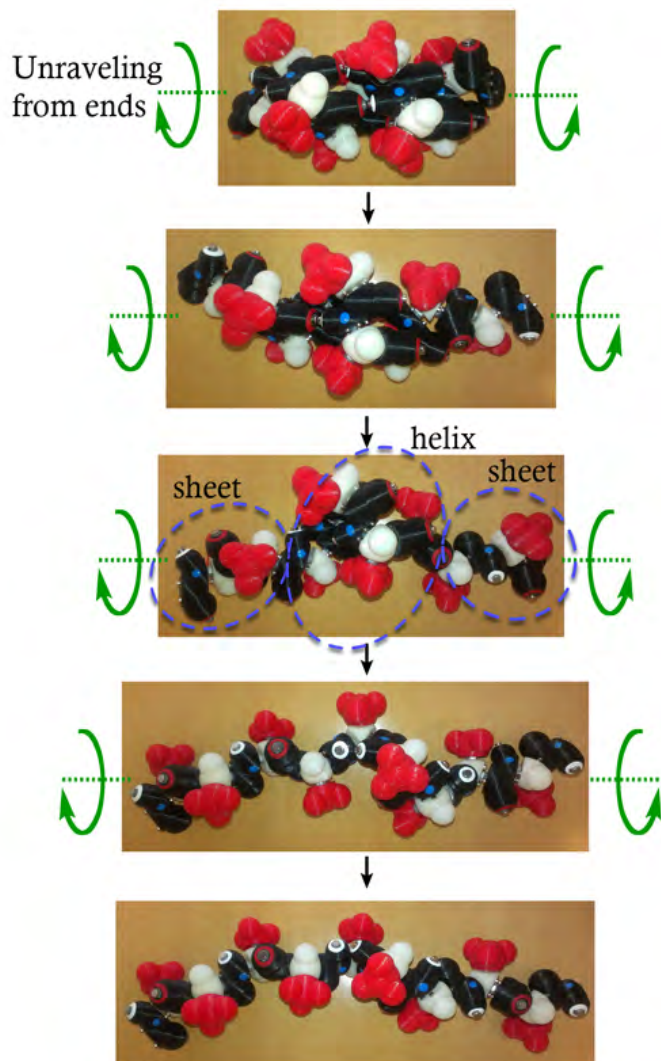
## Beta turns in Peppytides

$\beta$ -turns are one of the most commonly found secondary structures in proteins. We have explored Type I, I', II, II'  $\beta$ -turns with Peppytide (**Fig. S15**). These turn motifs were constructed with a glycine version of the model where the side chain methyl groups were removed.



**Fig. S15:**  $\beta$ -turns made with Peppytide. (a) Type I, (b) Type I', (c) Type II, (d) Type II'. (Left) Top-view of Peppytides parts assembled in CAD software to form  $\beta$ -turns. (Center) Front-view of Peppytides parts assembled in CAD software to form  $\beta$ -turns. (Right)  $\beta$ -turns made with the model.

## Unraveling of the alpha-helix model



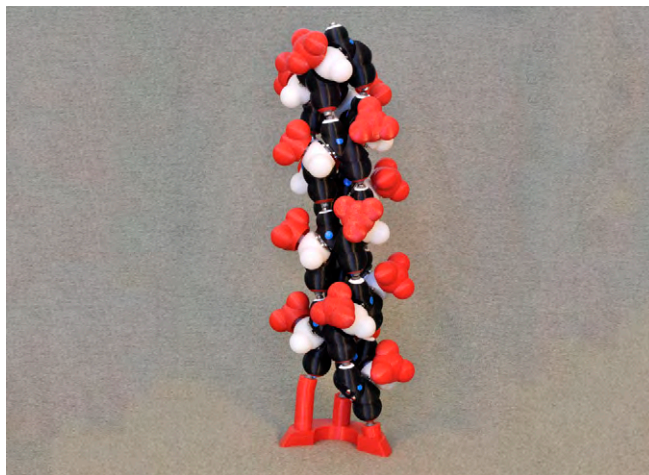
**Fig. S16:** Transition of  $\alpha$ -helix to  $\beta$ -sheet due to an applied torsional unraveling force on both sides.

## S7. Supplementary movie

Reference #	Filename	Description
Movie S1	pnas201305741_s2_17fsrm.mov	Folding the Peppytide model into an alpha-helix and an antiparallel beta sheet

# Supporting Information

Chakraborty and Zuckermann 10.1073/pnas.1305741110



**Movie S1.** This movie shows the folding of the Peppyptide physical model into protein secondary structure motifs. It demonstrates the conversion of an unstructured random coil into an  $\alpha$ -helix. It then shows unwinding of the helix, followed by formation of an antiparallel  $\beta$ -sheet.

[Movie S1](#)

## Other Supporting Information Files

[SI Appendix \(PDF\)](#)

[Dataset S1 \(TXT\)](#)

[Dataset S2 \(TXT\)](#)

[Dataset S3 \(TXT\)](#)